

**KAKATIYA UNIVERSITY**  
**M.A / M.Sc. MATHEMATICS Syllabus (w.e.f. 2019-20)**  
**Semester - I**  
**Paper – I**  
**Paper Code: M1CP1**  
**ALGEBRA**

**UNIT I**

Isomorphism theorems on Groups - Normal Series - **Solvable** groups - Nilpotent groups  
 (Chapter 5 : Sec 2 and Chapter 6 of Text Book 1)

**UNIT II**

Group Action on A set : The notation of a group action on a set - Isotropy subgroups - Orbits - Application of G-sets to counting.

Sylow Theorems: P-groups - Cauchy theorem - the Sylow theorems - Application of the Sylow theorems - Application to P-groups and the class equation - Further applications.

(Sec 16,17,36,37 of Text Book 2)

**UNIT III**

The field of quotients of an integral domain: The construction - Uniqueness.

Rings of Polynomials: Polynomials in an indeterminate – A review – The evaluation homomorphism - Factorization of polynomials over a field - The Division algorithm in  $F[x]$  - Irreducible Polynomials - Eisenstein criterion - Uniqueness of factorization in  $F[x]$  - Prime fields - Application to unique factorization in  $F[x]$ .

(Sec 21,22,23,27.17 to 27.27 of Text Book 2)

**UNIT IV**

Factorization: Unique factorization domains. Every PID is a UFD. If  $D$  is a UFD then  $D[x]$  is a UFD.

Euclidean Domains: Euclidean domains and Arithmetic in Euclidean domains.

Gaussian Integers and Multiplicative norms.

(Sect 45,46,47 of Text Book 2)

**Text Book:**

1. Basic Abstract Algebra by P.B. Bhattacharya, S.K.Jain, and S.R.Nagpaul, Second Edition, Cambridge University press.
2. A first Course in Abstract Algebra by John B.Fraleigh, Seventh Edition, Pearson education.

**Reference Books:**

1. Abstract Algebra by David S.Dummit, Richard M.Foote, Second edition, Wiley Student edition
2. Topics in Algebra by I.N Herstein
3. University algebra by N.Gopala Krishna.
4. Abstract Algebra by S.Lang.

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**Semester - I**  
**Paper – II**  
**Paper Code: M1CP2**  
**REAL ANALYSIS**

**UNIT I**

Metric Spaces: Limit points – Closed sets – Open sets – Perfect Sets – Bounded Sets – Closure of a set - Compact sets – Connected sets.

Numerical sequences in metric spaces: Subsequences – Cauchy sequence – Dia-meter of a set – Definition of complete metric space.

Continuous functions in metric spaces: Characterization of continuity in terms of open sets and closed sets, Continuity and Compactness.

(Sec 2.15, 2.16, 2.18 - 2.38, 2.44 – 2.47, 3.1, 3.2, 3.5, 3.6(a), 3.7 – 3.11(a), (b), 3.12, 4.5 – 4.8, 4.13, 4.14, 4.18, 4.19, 4.22 of Text Book)

**UNIT II**

The Riemann-Stieltjes Integral: Definitions of partition – Refinement of partition and RS-Integral, Necessary and Sufficient condition for integrability, Integral as a limit of a sum.

Integrability of continuous, Monotonic, discontinuous and composite functions.

Properties of the Integral: Integrability of sum and product of two functions – Integrability of modulus of a function – Integrators as step functions – Conversion of RS – Integral to Riemann integral.

(Sec 6.1 – 6.17, 6.19 of Text Book)

**UNIT III**

Sequences and Series of Functions: Pointwise and Uniform Convergence - Cauchy criterion for uniform convergence – Weirstrass  $M_n$  – test – Uniform convergence and Continuity – Uniform convergence and Integrability –Uniform convergence and differentiability - Equi continuous families of functions

(Sec 7.1 – 7.14, 7.16 – 7.25 of Text-book)

**UNIT IV**

Weirstrass approximation theorem – Definition of uniformly closed algebra – Stone's generalization of the Weirstrass theorem.

Power Series: Radius of Convergence – Real Power Series – Continuity and Differentiability of Power Series – Abel's theorem – inversion in the order of summation - Taylor's theorem – Identical power series.

(Sec 3.38 – 3.40, 7.26 – 7.32, 8.1 – 8.5 of Text-book)

**Text Book:**

Principles of Mathematical Analysis by Walter Rudin, McGraw – Hill, 3<sup>rd</sup> Edition

**Reference Books:**

1. Mathematical Analysis by S.C.Malik and Savita Arora, S.Chand, 4<sup>th</sup> Edition
2. Mathematial Analysis by T.Apostle, Narosa.

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**Semester – I**  
**Paper – III**  
**Paper Code: M1CP3**  
**ORDINARY DIFFERENTIAL EQUATIONS**

**UNIT I**

**Integration in series** : Ordinary and singular points – power series solution at ordinary point- Frobenius method – Problems on type I , type II , type III and type IV – series solution about regular singular point at infinity.

(Chapter 8: Sec 8.1 to 8.14 of Text Book 1)

**UNIT II**

**Linear equations with variable coefficients**: Introduction – Initial value problem for homogeneous equation – The Wronskian and linear dependence – reduction of the order of homogeneous equation – The non homogeneous equation.

(Sec 3.1 to 3.6 of Text Book 2)

**UNIT III**

**Existence and uniqueness of solution of first order equation**: The method of successive approximation – The Lipschitz condition – Sturm-Liouville problem – Orthogonality of eigen functions and Reality of eigen functions.

(Sec 5.4 to 5.5 of Text Book 2 and Sec 15.10 to 15.12 of Text Book 1)

**UNIT IV**

**Variational problems with fixed boundaries**: Euler's equation for functional containing first order derivative and one independent variable – Extremals – Functional dependent on higher order derivatives – Functions dependent on more than one independent variable – Variational problem in parametric form – Invariance of Euler's equation under coordinate transformation.

(Chapter 1 of part V of Text Book 1)

**Text book**

1. Advanced differential equations, M.D. Raisingania, S.Chand Company Ltd.
2. An introduction to ordinary differential equations by E.A. Coddington  
Prentice-Hall of India Pvt. Ltd.

**Referene books :**

1. Differential equations with applications and Historical notes by George F. Simmons
2. Theory of ordinary differential equations by Somasundaram – Narosa.

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**Semester - I**  
**Paper – IV**  
**Paper code: M1CP4**  
**DISCRETE MATHEMATICS**

**UNIT I: Fundamentals of Logic**

Fundamentals of logic-Logical inferences - Methods of proof of an implication – First order logic and other methods of proof - Rules of inference for propositions - Rules of inference for quantified propositions.

(Sec 1.5, 1.6, 1.7, 1.8 up to De Morgan Laws, 1.9 of Text Book)

**UNIT II: Permutations and Combinations**

Enumerating combinations and permutations with repetitions- Enumerating permutations with constrained repetitions- The principle of inclusion and exclusion.

(Sec 2.1 to 2.5, 2.8 of Text Book)

**UNIT III: Recurrence Relations**

Generating function of sequences – Calculating coefficients of generating functions- Recurrence relations- Solving recurrence relations by substitution and generating functions- the method of characteristic roots – solutions of inhomogeneous recurrence relations.

(Sec 3.1 to 3.6 of Text Book)

**UNIT IV: Boolean Algebra**

Introduction, Boolean algebras – Boolean polynomials – Disjunctive and Conjunctive normal forms – Switching functions.-minimization of switching functions.

(Sec 6.1 to 6.5 of Text Book)

**Text Book:**

Discrete Mathematics for Computer Scientists and Mathematicians by J.L.Mott, A. Kandel, and T.P. Baker

**Reference Books:**

1. Discrete Mathematical structures by Roden.
2. Discrete Mathematics by Kolman.
3. A Text book of Discrete Mathematics by Tremblay and Manohar.
4. Elements of Discrete Mathematics by C.L.Liu, McGraw Hill Company

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**Semester - I**  
**Paper – V**  
**Paper Code: M1CP5**  
**FUNDAMENTALS OF STATISTICS**

**UNIT I**

Moments–Pearson’s  $\beta$  and  $\gamma$  coefficients -Skewness and Kurtosis  
Probability Definitions–Addition Theorem-Conditional probability - Multiplication Law of probability - Baye’s Theorem - Random Variables - Probability mass function – Probability density function.  
(Chapter 2, 3, 4.2, 5.1 to 5.5.5 of Text Book)

**UNIT II**

Mathematical Expectation – Expectation of a function of a random variable – Addition and Multiplication theorem of expectation - Expectation of linear Combination of random variables – Covariance – Variance of linear combination on of random variables – Moment generating function – Chebychev’s inequality – Correlation –Karl Pearson’s coefficient of Correlation- Linear regression.Angle between two regression lines.  
(Chapter 6.1 to 6.6.1, 7.1, 7.1.2, 7.5,10.1 to 10.4.2, 11.1 to 11.2.3 of Text Book)

**UNIT III**

Discrete Distributions - Bernoulli distribution – Moments of Bernoulli distribution – Binomial distribution – Moments - Moment generating function of Binomial distribution – Additive property of Binomial distribution - Poisson distribution – Moments of Poisson distribution – Geometric distribution –Lack of memory property.  
(Chapter 8.1 to 8.4.1, 8.4.4 to 8.4.7, 8.5, 8.5.2, 8.5.3, 8.5.5, 8.5.8, 8.7 to 8.7.3 of Text Book)

**UNIT IV**

Continuous Distributions -Normal Distribution – Characteristics of Normal Distribution and normal probability curve - Moments of Normal Distribution – Area property- Gamma Distribution - Moment generating function of Gamma Distribution – Exponential distribution- Moment generating function of Exponential distribution- Lack of memory property.  
(Chapter 9.1, 9.2, 9.2.2 to 9.2.5, 9.2.7 to 9.2.11, 9.5, 9.5.1, 9.5.3, 9.8, 9.8.1 of Text Book)

**Text Book:**

Fundamentals of Mathematical Statistics by S.C. Gupta & V.K.Kapoor, 11<sup>th</sup> Edition